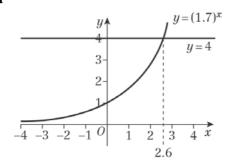
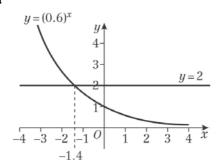
Exponentials and logarithms 14A

1 a



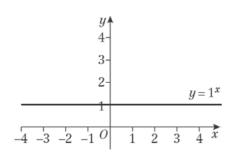
b Where y = 4, $x \approx 2.6$

2 a



b Where $y = 2, x \approx -1.4$

3



4 a True because, when x = 0, $a^0 = 1$ when a is positive

b False. For example, when $a = \frac{1}{2}$, the function $f(x) = a^x$ is not an increasing function.

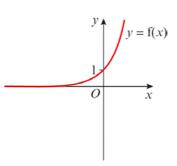
c True because, when *a* is positive, $a^x > 0$ for all values of *x*.

5 a The graph crosses the y-axis when

$$x = 0.$$

$$y = 3^{0}$$
So $y = 1$

The graph crosses the y-axis at (0, 1). Asymptote is at y = 0.



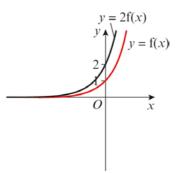
b The graph is a vertical stretch by scale factor 2.

The graph crosses the y-axis when

$$x = 0.$$
$$y = 2 \times 3^0$$

So
$$y = 2$$

The graph crosses the y-axis at (0, 2). Asymptote is at y = 0.



 ${f c}$ The graph is a translation by the

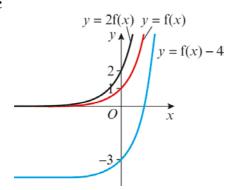
vector
$$\begin{pmatrix} 0 \\ -4 \end{pmatrix}$$

The graph crosses the *y*-axis when x = 0.

$$y = 3^0 - 4$$

So
$$y = -3$$

The graph crosses the y-axis at (0, -3). Asymptote is at y = -4. 5 c



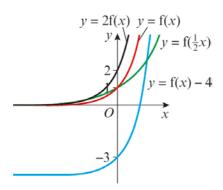
d The graph is a horizontal stretch by scale factor 2.

The graph crosses the *y*-axis when x = 0.

$$y = 3^{\frac{1}{2} \times 0}$$

So
$$y = 1$$

The graph crosses the y-axis at (0, 1). Asymptote is at y = 0.



Substitute the coordinates into $y = ka^x$. $6 = ka^1$ (equation 1)

 $48 = ka^4$ (equation 2)

Solve simultaneously: divide equation 2 by equation 1

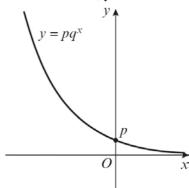
2 by equation 1,

$$48 \div 6 = \frac{ka^4}{ka}$$

$$a^3 = 8$$

$$a = 2, k = 3$$

7 a As x increases, y decreases



b Substitute the coordinates into $y = pq^x$.

$$150 = pq^{-3}$$
 (equation 1)

$$0.048 = pq^2$$
 (equation 2)

Solve simultaneously, divide equation 2 by equation 1.

$$0.048 \div 150 = \frac{pq^2}{pq^{-3}}$$

$$a^5 = 0.00032$$

$$q = 0.2$$

$$p = 0.048 \div 0.2^2 = 1.2$$

$$p = 1.2, q = 0.2$$

Challenge

To draw the graph, note that it is a translation of the graph $y = 2^x$ by the vector $\begin{pmatrix} 2 \\ 5 \end{pmatrix}$.

The graph crosses the *y*-axis when x = 0, so $y = 2^{0-2} + 5$

$$y = 5.25$$

The graph crosses the y-axis at (0, 5.25). Asymptote is at y = 5.

